

Syntax-Directed Derivative Code (Part I: Tangent-Linear Code)

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Abstract. This is the first instance in a series of papers on single-pass generation of various types of derivative code by syntax-directed translation. We consider the automatic generation of tangent-linear code by forward mode automatic differentiation implemented as the bottom-up propagation of synthesized attributes on the abstract syntax tree. A proof-of-concept implementation is presented based on a simple LALR(1) parser generated by the parser generator `bison`. The proposed technique can be generalized easily to provide a method for computing directional derivatives of mathematical vector functions that are implemented as computer programs in the context of computer algebra systems and compilers for scientific computing. The main advantage of the syntax-directed approach to automatic differentiation is its elegance in terms of the implementation.

1 Motivation and Summary of Results

This paper presents a method for generating *tangent-linear* versions of numerical simulation programs¹ that implement vector functions

$$F : \mathbb{R}^n \rightarrow \mathbb{R}^m, \quad \mathbf{y} = F(\mathbf{x}), \quad \mathbf{x} = (x_k)_{k=1,\dots,n}, \quad \mathbf{y} = (y_l)_{l=1,\dots,m} \quad , \quad (1)$$

automatically by syntax-directed translation. Such tangent-linear programs $\dot{F} = \dot{F}(\mathbf{x}, \dot{\mathbf{x}})$ compute directional derivatives $\dot{\mathbf{y}}$, that is, products of the Jacobian matrix

$$F' = (f'_{l,k})_{k=1,\dots,n}^{l=1,\dots,m} \equiv \left(\frac{\partial y_l}{\partial x_k} \right)_{k=1,\dots,n}^{l=1,\dots,m} \in \mathbb{R}^{m \times n} \quad (2)$$

with a direction $\dot{\mathbf{x}}$ in the input space \mathbb{R}^n . Formally,

$$\dot{\mathbf{y}} = \dot{F}(\mathbf{x}, \dot{\mathbf{x}}) \equiv F' \cdot \dot{\mathbf{x}} \quad . \quad (3)$$

To motivate the need for tangent-linear codes we consider a system of nonlinear equations

$$F(\mathbf{x}) = 0, \quad F : \mathbb{R}^n \rightarrow \mathbb{R}^n \quad . \quad (4)$$

Given a good start estimate \mathbf{x}^0 , the system can be solved by Newton's method with quadratic convergence as follows:

$$\begin{aligned} \delta \mathbf{x}^i &= -(F'(\mathbf{x}^i))^{-1} \cdot F(\mathbf{x}^i) \\ \mathbf{x}^{i+1} &= \mathbf{x}^i + \delta \mathbf{x}^i \end{aligned}$$

for increasing integer values i . At each step the algorithm requires the Jacobian F' of F at the current estimate \mathbf{x}^i . Finite difference quotients can be used to

¹ Without loss of generality, we focus on a subset of C.

approximate the entries of the Jacobian at the cost of $n + 1$ and $2n$ function evaluations when using forward (or backward) and centered differences, respectively. However, it is well-known that step size control is a problem as illustrated in Figure 1 and discussed, for example, in [13]. To avoid these problems, the tangent-linear program can be run with \mathbf{x} ranging over the Cartesian basis vectors in \mathbb{R}^n to obtain F' at roughly the same cost as that of (centered) finite differences but with machine accuracy.

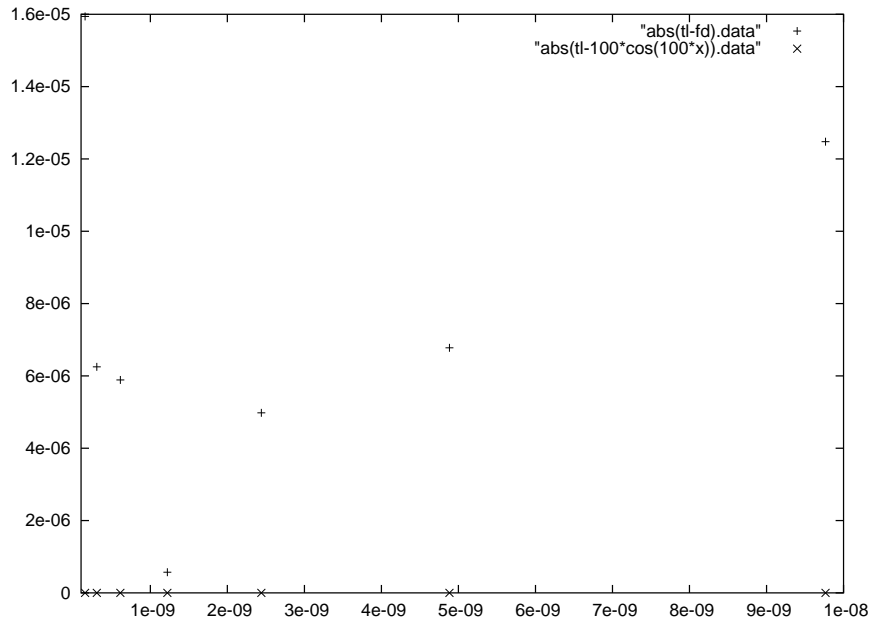


Fig. 1. Problems with finite differences: We show the absolute error of finite difference approximation of $\frac{\partial y}{\partial x}$ for $y = \sin(100 * x)$ at $x = 0.5$ and $h \in (10^{-10}, 10^{-8})$ (marked with "+" symbols). The values computed by the tangent-linear code are identical with those of the hand-coded derivative (correct up to machine accuracy) $\frac{\partial y}{\partial x} = 100 * \cos(100 * x)$. The "x" points mark the vanishing absolute error for this case.

Choosing a matrix-free approach, the Newton step can be obtained as the solution of the linear system

$$F'(\mathbf{x}^i) \delta \mathbf{x}^i = -F(\mathbf{x}^i) \quad (5)$$

at each Newton iteration i . Direct methods may be prohibitive due to the potentially large size of the problem. Iterative methods are likely to be more suitable. For example, iterative refinement computes the iterates as

$$\delta \mathbf{x}^{i+1} = \delta \mathbf{x}^i + B(F(\mathbf{x}^i) - F'(\mathbf{x}^i) \cdot \delta \mathbf{x}^i) \quad (6)$$

for a suitable preconditioner B , such as an approximate inverse of $F'(\mathbf{x}^i)$. Note that Equation (6), as well as matrix-free Krylov methods such as GMRES, involves the computation of the product of the Jacobian with a vector. A (forward) finite difference approximation of the Jacobian vector product in Equation (3) can be computed by perturbing the scalar input of the modified function

$$\tilde{F} : \mathbb{R} \rightarrow \mathbb{R}^m, \quad \tilde{\mathbf{y}} = \tilde{F}(s) \equiv F((s - 1) \cdot \mathbf{x} + \mathbf{x}) \quad (7)$$

at $s = 1$.² Hence, we compute $\mathbf{y} = F(\mathbf{x})$ and $\mathbf{y}' = F(h \cdot \dot{\mathbf{x}} + \mathbf{x})$ to get

$$\dot{\mathbf{y}} \approx \frac{\mathbf{y}' - \mathbf{y}}{h} \quad .$$

There is no need to form the whole Jacobian explicitly. Additional scaling in dependence of the value of a norm of $\dot{\mathbf{x}}$ may be required to avoid numerical instabilities as pointed out, for example, in [14]. Moreover, the usual problems with finite differences may occur. Tangent-linear codes should be used in order to circumvent both problems.

The structure of this paper is as follows. In Section 2 we summarize the theoretical concepts behind forward mode automatic differentiation in the context of tangent-linear code generation by source transformation. The syntax-directed translation algorithm for straight-line programs is introduced in Section 3 – the heart of this paper. Generalizations for subroutines with intraprocedural flow of control and programs with interprocedural flow of control are discussed. A simple proof-of-concept implementation is presented in Section 4, making detailed references to the source code that is appended in Section A. We draw conclusions in Section 5 and give an outlook to part II of this paper which deals with the syntax-directed generation of adjoint code.

2 Fundamentals

For a given implementation of a vector function as defined in Equation (1) as a computer program³ we use *automatic differentiation (AD)* [17], [9]⁴ by source transformation to generate code for computing directional first derivatives of F . Therefore the computation of $\mathbf{y} = F(\mathbf{x})$ is expected to decompose into a sequence of elemental assignments

$$v_j = \varphi_j(v_i)_{i \prec j} \quad (8)$$

for $j = 1, \dots, p+m$, and $i \prec j$ if and only if v_i is an argument of φ_j . Equation (8) is also referred to as the *code list* of F . We set $v_{i-n} = x_i$ for $i = 1, \dots, n$ and $v_{p+j} = y_j$ for $j = 1, \dots, m$. The v_k , $k = 1-n, \dots, p+m$, are called *code list variables*. Forward mode AD transforms F into the tangent-linear model \tilde{F} that computes a total (or directional) derivative as defined in Equation (3). The $m \times n$ Jacobian of F is defined in Equation (2). The transformation of the program semantics is achieved by applying well-known differentiation rules to the *elemental* functions

$$\varphi_j \in \{+, -, *, /, \sin, \exp, \dots\}^5$$

² The basic idea is the following: We need

$$\frac{\partial x_i}{\partial s} = \dot{x}_i$$

for $i = 1, \dots, n$. Therefore, we set $\mathbf{x} = \dot{\mathbf{x}} \cdot s + \tilde{\mathbf{x}}$ to determine suitable values for $\tilde{\mathbf{x}}$. For $s = 1$ the right-hand side of $\tilde{\mathbf{x}} \equiv \mathbf{x} - \dot{\mathbf{x}}$ can be substituted in $F(\mathbf{x})$ to get Equation (7).

³ From now on we will use F to refer to this implementation as a computer program.

⁴ We follow the notation therein as closely as possible.

⁵ We consider a subset of the arithmetic operators and intrinsic functions provided by most programming languages.

followed by the exploitation of the chain rule as

$$\dot{v}_j = \sum_{i \prec j} c_{ji} \cdot \dot{v}_i \quad (9)$$

for $j = 1, \dots, p + m$ and total derivatives \dot{v}_k of the code list variables v_k , $k = 1 - n, \dots, p + m$. The elemental functions φ_j are assumed to be continuously differentiable in a neighborhood of the current argument. The corresponding local partial derivatives are denoted by

$$c_{ji} = \frac{\partial \varphi_j}{\partial v_i} \quad \text{for } j = 1, \dots, p + m, \quad i \prec j \quad ,$$

where the *independent* variables $v_{i-n} = x_i$, $i = 1, \dots, n$, are assumed to be mutually independent. The basic approach dates back to [19]. Since then, AD has been used in the context of a large number of projects in computational science and engineering providing fast and accurate derivative information for a wide variety of highly relevant applications. Many of them are documented in the proceedings of the four international conferences [7], [2], [6], and [5]. Source transformation tools for AD (see, for example, ADIFOR [3], ADIC [4], the differentiation-enabled NAGWare Fortran 95 compiler [16], TAPENADE [12], TAF [8], and OpenAD [20]) that provide a basic forward mode generate tangent-linear code as an augmentation of the code list by statements for computing directional derivatives as illustrated by the following example which shows the tangent-linear code of " $y = \sin(x * 2)$ ".

$$\begin{array}{ll} \dot{v}_1 = \dot{x} & v_1 = x \\ \dot{v}_2 = 0 & v_2 = 2 \\ \dot{v}_3 = \dot{v}_1 * v_2 + v_1 * \dot{v}_2 & v_3 = v_1 * v_2 \\ \dot{v}_4 = \cos(v_3) * \dot{v}_3 & v_4 = \sin(v_3) \\ \dot{y} = \dot{v}_4 & y = v_4 \quad . \end{array}$$

Less trivial examples follow after explaining the syntax-directed approach to the generation of tangent-linear code in the following section.

3 Syntax-Directed Tangent-Linear Codes

The main conceptual issues of the syntax-directed construction of tangent-linear codes can be discussed in the context of simple sequences of scalar assignments as defined in Definition 1. The presence of control-flow structures – both intra- (loops, branches, or arbitrary jumps in the form of `goto` statements) and inter-procedural (subroutine calls and calls of user-defined functions) – adds little to the algorithmic details behind the proposed method as explained in Section 3.4 and in Section 3.5.

Definition 1. A straight-line program (SLP) is a sequence of scalar assignments described by the context-free grammar $G = (N, T, P, s)$ with nonterminal symbols

$$N = \{ s \text{ (straight-line program)} \quad a \text{ (assignment)} \quad e \text{ (expression)} \quad \}$$

terminal symbols

$$T = \left\{ \begin{array}{l} V \text{ (program variables; see line 16 in Section A.2, Listing 1.5)} \\ C \text{ (constants; line 21)} \\ F \text{ (unary intrinsic; line 15)} \\ O \text{ (binary operator; line 27)} \\ , ;) (\text{ (remaining single character tokens; line 27)} \end{array} \right\}$$

start symbol s , and production rules

$$P = \left\{ \begin{array}{ll} (P1) & s :: a \quad \text{(see line 32 in Section A.3, Listing 1.6)} \\ (P2) & s :: as \quad \text{(line 36)} \\ (P3) & a :: V = e; \quad \text{(line 68)} \\ (P4) & e :: V \quad \text{(line 102)} \\ (P5) & e :: C \quad \text{(line 109)} \\ (P6) & e :: F(e) \quad \text{(line 94)} \\ (P7) & e :: eOe \quad \text{(line 76 and line 85)} \end{array} \right\}$$

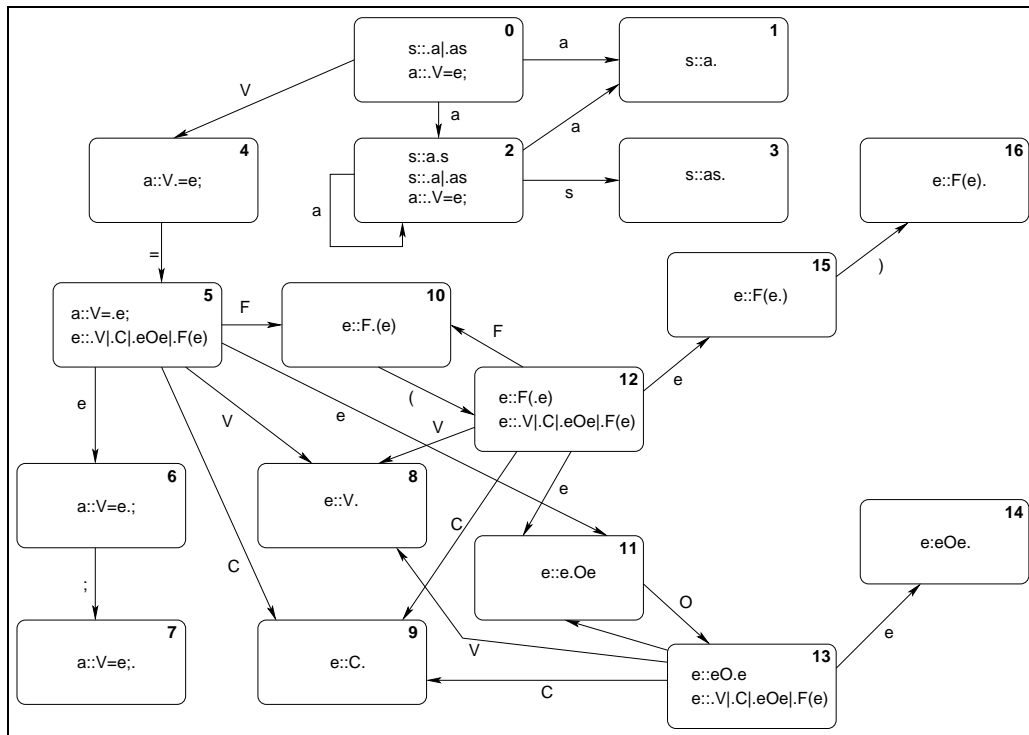


Fig. 2. Characteristic finite automaton of SLPs

References to the source code of a simple proof-of-concept implementation (see also Section 4) are given for terminal symbols (references into the grammar configuration file of the lexical analyzer) and production rules (references into the grammar configuration file of the syntax analyzer).

By considering unary intrinsics and binary arithmetic operators we cover a large fraction of the elemental functions provided by modern programming languages. A generalization to include other potentially relevant cases such as unary operators or intrinsics that take more than one argument complicates the grammar and thus the parsing procedure while not adding anything conceptual to the approach of generating tangent-linear code by syntax-directed translation. Hence we decided to limit the amount of syntax to a minimum that allows us to introduce the theoretical idea behind syntax-directed compilation of tangent-linear code and to verify the numerical correctness of the generated code. The latter is done by comparing the values of the directional derivatives with approximations obtained by finite difference quotients as described in Section 4.

Programs come as sequences of ASCII characters that need to be transformed into a structured form to allow for semantic transformation according to well-defined syntactic rules. A lexical analyzer is used to partition the input code into a sequence of tokens that correspond to terminal symbols in Definition 1. The correctness of the input in form of the token stream is verified by a shift-reduce parser. See [1] for the technical details. We use an LALR(1)-parsing algorithm based on a *push-down automaton (PDA)* $A = (\alpha, \sigma)$ that consists of a *characteristic finite automaton (CFA)* α and a *shift-reduce stack (SRS)* σ to store states of α . The CFA $\alpha = (V_\alpha, E_\alpha)$ of an SLP is defined as follows

$$V_\alpha = \left\{ \begin{array}{l} 0 = [a|as|V = e;] \quad 1 = [\mathbf{P1}] \quad 2 = [s|a|as|V = e;] \\ 3 = [\mathbf{P2}] \quad 4 = [= e;] \quad 5 = [e;|V|C|F(e)|eOe] \\ 6 = [;] \quad 7 = [\mathbf{P3}] \quad 8 = [\mathbf{P4}] \\ 9 = [\mathbf{P5}] \quad 10 = [(e)] \quad 11 = [Oe] \\ 12 = [e]|V|C|F(e)|eOe \quad 13 = [e|V|C|F(e)|eOe] \quad 14 = [\mathbf{P6}] \\ 15 = [] \quad 16 = [\mathbf{P7}] \end{array} \right\} \quad (10)$$

$$E_\alpha = \left\{ \begin{array}{l} (0,1)[a], (0,2)[a], (0,4)[V] \\ (2,1)[a], (2,2)[a], (2,3)[s] \\ (4,5)[=] \\ (5,6)[e], (5,8)[V], (5,9)[C], (5,10)[F], (5,10)[e] \\ (6,7)[;] \\ (10,12)[(] \\ (11,13)[O] \\ (12,8)[V], (12,9)[C], (12,10)[F], (12,11)[e], (12,15)[e] \\ (13,8)[V], (13,9)[C], (13,10)[F], (13,11)[e], (13,14)[e] \\ (15,16)[)] \end{array} \right\} \quad (11)$$

The symbol "|" is used to separate alternative parts of right-hand sides of the production rules that are associated with the CFA vertices. The CFA is non-deterministic. A graphical representation is given in Figure 2. A lookahead of one on the input token stream is required to make it deterministic. The lookahead is realized by the function $\lambda \equiv \lambda(f, i) \in T$ that returns for the given position i in an SLP the next token.

3.1 Example

We use the PDA to construct the abstract syntax tree (AST) $\mathbf{A} = (\mathbf{V}, \mathbf{E})$ of the assignment ” $y = \sin(x * 2);$ ” which is transformed by the lexical analyzer into the token stream

$$”V = F(VOC);” \quad .$$

A representation of the parse table is shown in Table 1. The AST \mathbf{A} can be

	σ	$i \in V_a$	Read	Action	λ	Line
1		0	V	S		68
2		0	4 V =	S		68
3		0,4	5 V = F	S		94
4		0,4,5	10 V = F(S		94
5		0,4,5,10	12 V = F(V	S		94
6		0,4,5,10,12	8	R(P4)		102
7		0,4,5,10	12 V=F(e	S	O	94
8		0,4,5,10,12	11 V=F(eO	S		76
9		0,4,5,10,12,11	13 V=F(eOC	S		76
10		0,4,5,10,12,11,13	9	R(P5)		109
11		0,4,5,10,12,11	13 V=F(eOe	S)	76
12		0,4,5,10,12,11,13	14	R(P7)		76
13		0,4,5,10	12 V=F(e	S)	94
14		0,4,5,10,12	15 V=F(e)	S		94
15		0,4,5,10,12,15	16	R(P6)		94
16		0,4	5 V=e	S	;	68
17		0,4,5	6 V=e;	S		68
18		0,4,5,6	7	R(P3)		68
19			0 a	S	\emptyset	32
20		0	1	R(P1)		32
21			0 s			23

Table 1. Extended Parse Table: A total of 21 shift (S in ”Action” column) or reduce (R in ”Action” column together with the production rule that is matched) operations are performed. We show the contents of the stack σ , the current state i in the characteristic finite automaton, the string read so far, the lookahead token λ , and the corresponding line number in the parser configuration file in Section A.3, Listing 1.6. In row 19 we get empty lookahead \emptyset as a result of the sequence of assignments containing only a single element.

extracted by applying the reduce operations in reverse order. It is shown in Figure 3.

3.2 Code List

The first step of the compilation of tangent-linear code is to break complex right-hand sides of assignments down to elemental assignments by constructing statement-level code lists. Initializing $j = \nu = 1$ we extend the production rules by custom reduce actions as shown in Figure 4. We use the increment operator $j++$ as defined in the C standard. Otherwise, the addition ”+” serves as a string concatenation operator. All actions performed are purely symbolic in the sense that they derive new strings from given ones according to well-defined rules stated in Section 2. The attribute a that is associated with all vertices in the AST is synthesized via concatenation of strings during the bottom-up parsing.

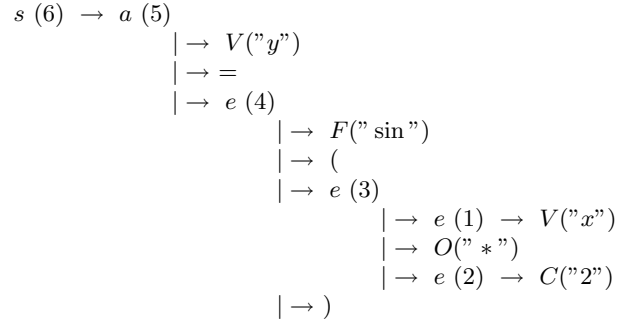


Fig. 3. AST of " $V = F(VOC);$ ".

$$P_{cl} = \left\{ \begin{array}{l}
(P1) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a \\
\quad \nu++ \\
(P2) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\mu_1}.a + \mathbf{v}_{\mu_2}.a \\
\quad \text{where } \mathbf{v}_{\mu_1} \hat{=} a \text{ and } \mathbf{v}_{\mu_2} \hat{=} s \text{ in } as \\
\quad \nu++ \\
(P3) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a + V.a + " = " + "v_{[\mathbf{v}_{\nu-1}.j]} + "; \\
\quad c = 1; \nu++ \\
(P4) \quad \mathbf{v}_\nu.a = "v_{[c]} + " = " + V.a + "; \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
(P5) \quad \mathbf{v}_\nu.a = "v_{[c]} + " = " + C.a + "; \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
(P6) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a + "v_{[c]} + " = " \\
\quad + F.a + "(" + "v_{[\mathbf{v}_{\nu-1}.j]} + "; \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
(P7) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\mu_1}.a + \mathbf{v}_{\mu_2}.a + "v_{[c]} + " = " \\
\quad + "v_{[\mathbf{v}_{\mu_1}.j]} + O.a + "v_{[\mathbf{v}_{\mu_2}.j]} + "; \\
\quad \text{where } \mathbf{v}_{\mu_1} \hat{=} e^1 \text{ and } \mathbf{v}_{\mu_2} \hat{=} e^2 \text{ in } e^1 O e^2 \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++
\end{array} \right.$$

Fig. 4. Production rules for syntax-directed compilation of assignment-level code lists for SLPs. We use the notation " $\hat{=}$ " in the sense of "corresponds to," that is for example, \mathbf{v}_{μ_1} is the vertex in the AST that corresponds to the first non-terminal on the right-hand side of rule (P2).

It contains the code list of the previously parsed part of the code, respectively. The second attribute j is used to store the index of the corresponding code list variable inside of expressions on the right-hand side of assignments. Expressions in square brackets depend on one of the algorithm's counters c or ν . They need to be transformed into the corresponding string, for example, " $v_{[\mathbf{v}_{\nu-1}.j]}$ " becomes " v_3 " if the value of the j -attribute of $\mathbf{v}_{\nu-1} \in \mathbf{V}$ is equal to 3.

To improve the structure of the output one may think of a semicolon at the end of an assignment as followed by a newline character (see implementation in Section 4). For example, the application of the symbolic rules in Figure 4 to " $y = \sin(x * 2);$ " proceeds as follows.

- (P4 with $\nu = 1$, $[c] = 1$, and $V.a = "x"$)
- (P5 with $\nu = 2$, $[c] = 2$, and $C.a = "2"$)
- (P7 with $\nu = 3$, $\mu_1 = 1$, $\mu_2 = 2$,
 $\mathbf{v}_{\mu_1}.a = "v_1 = x;"$, $\mathbf{v}_{\mu_2}.a = "v_2 = 2;"$, $[c] = 3$,
 $[\mathbf{v}_{\mu_1}.j] = 1$, $O.a = "*"$, and $[\mathbf{v}_{\mu_2}.j] = 2$)
- (P6 with $\nu = 4$, $\mathbf{v}_{\nu-1}.a = "v_1 = x;"$
 $v_2 = 2;$
 $v_3 = v_1 * v_2;"$,
 $[c] = 4$, $F.a = "sin"$, and $[\mathbf{v}_{\nu-1}.j] = 3$)
- (P3 with $\nu = 5$, $\mathbf{v}_{\nu-1}.a = "v_1 = x;"$
 $v_2 = 2;$
 $v_3 = v_1 * v_2;$
 $v_4 = \sin(v_3);"$,
 $V.a = "y"$, and $[\mathbf{v}_{\nu-1}.j] = 4$)
- (P1 with $\nu = 6$, $\mathbf{v}_{\nu-1}.a = "v_1 = x;"$
 $v_2 = 2;$
 $v_3 = v_1 * v_2;$
 $v_4 = \sin(v_3);$
 $y = v_4;"$)

The complete AST is available after the last reduction operation ($P1$) that is performed by the shift-reduce parsing procedure in Table 1. Hence, the synthesized attribute $\mathbf{v}_6.a$ contains the entire code list in form of a copy of $\mathbf{v}_5.a$.

3.3 Tangent-Linear SLP

Tangent-linear code is constructed by augmenting the code list locally with statements for computing directional derivatives of the elemental functions. The production rules for syntax-directed compilation of tangent-linear SLPs are shown in Figure 5. We use the notation $V.\dot{a}$ to refer to the string that marks the directional derivative component of the variable marked by the string $V.a$, that is, if

$$P_{tlc} = \left\{ \begin{array}{l}
(P1) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a \\
\quad \nu++ \\
\quad \text{(See lines 32–35 in Section A.3, Listing 1.6.)} \\
(P2) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\mu_1}.a + \mathbf{v}_{\mu_2}.a \\
\quad \text{where } \mathbf{v}_{\mu_1} \hat{=} a \text{ and } \mathbf{v}_{\mu_2} \hat{=} s \text{ in } as \\
\quad \nu++ \\
\quad \text{(See lines 36 – 42.)} \\
(P3) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a + V.\dot{a} + " = " + " \dot{v}_{[\mathbf{v}_{\nu-1}.j]} " + "; " \\
\quad + V.a + " = " + " v_{[\mathbf{v}_{\nu-1}.j]} " + "; " \\
\quad c = 1; \nu++ \\
\quad \text{(See lines 68 – 75.)} \\
(P4) \quad \mathbf{v}_\nu.a = " \dot{v}_{[c]} " + " = " + V.\dot{a} + "; " \\
\quad + " v_{[c]} " + " = " + V.a + "; " \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
\quad \text{(See lines 102 – 108.)} \\
(P5) \quad \mathbf{v}_\nu.a = " \dot{v}_{[c]} " + " = 0; " \\
\quad + " v_{[c]} " + " = " + C.a + "; " \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
\quad \text{(See lines 109 – 114.)} \\
(P6) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\nu-1}.a + " \dot{v}_{[c]} " + " = " \\
\quad + \frac{\partial F.a}{\partial " v_{[\mathbf{v}_{\nu-1}.j]} " } + " (" + " \dot{v}_{[\mathbf{v}_{\nu-1}.j]} " + "); " \\
\quad + " v_{[c]} " + " = " \\
\quad + F.a + " (" + " v_{[\mathbf{v}_{\nu-1}.j]} " + "); " \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
\quad \text{(See lines 94 – 101.)} \\
(P7) \quad \mathbf{v}_\nu.a = \mathbf{v}_{\mu_1}.a + \mathbf{v}_{\mu_2}.a + " \dot{v}_{[c]} " + " = " \\
\quad + " \dot{v}_{[\mathbf{v}_{\mu_1}.j]} " + " * " + \frac{\partial O.a}{\partial " v_{[\mathbf{v}_{\mu_1}.j]} " } + " + " \\
\quad + \frac{\partial O.a}{\partial " v_{[\mathbf{v}_{\mu_2}.j]} " } + " * " + " \dot{v}_{[\mathbf{v}_{\mu_2}.j]} " + " ; " + " v_{[c]} " \\
\quad + " = " + " v_{[\mathbf{v}_{\mu_1}.j]} " + O.a + " v_{[\mathbf{v}_{\mu_2}.j]} " + "; " \\
\quad \text{where } \mathbf{v}_{\mu_1} \hat{=} e^1 \text{ and } \mathbf{v}_{\mu_2} \hat{=} e^2 \text{ in } e^1 O e^2 \\
\quad \mathbf{v}_\nu.j = c++ \\
\quad \nu++ \\
\quad \text{(See lines 76 – 84 and 85 – 93.)}
\end{array} \right.$$

Fig. 5. Production rules for syntax-directed compilation of tangent-linear SLPs.

$V.a = "x"$, then $V.\dot{a} = "\dot{x}"$. In (P6) the symbolic transformation

$$\frac{\partial F.a}{\partial "v_{[\mathbf{v}_{\nu-1}.j]}"}$$

is defined according to the differentiation rules of the elemental functions, for example, if $F.a = " \sin "$ and $"v_{[\mathbf{v}_{\nu-1}.j]} = "v_1"$, then

$$\frac{\partial F.a}{\partial "v_{[\mathbf{v}_{\nu-1}.j]}"} = \frac{\partial " \sin(v_1)"}{\partial "v_1"} = " \cos(v_1) " \quad .$$

We assume that partial derivatives of unary intrinsics are again unary functions of the same argument. The symbolic rule can be modified to account for deviations, for example,

$$\frac{\partial " \exp "} {\partial "v_{[\mathbf{v}_{\nu-1}.j]}"} = "v_{[\mathbf{v}_{\nu}.j]} " \quad .$$

Similarly, in (P7)

$$\frac{\partial O.a}{\partial "v_{[\mathbf{v}_{\mu_1}.j]}"} = "v_{[\mathbf{v}_{\mu_2}.j]} "$$

if $O.a = " * "$.

The generation of the tangent-linear code for $"y = \sin(x * 2);"$ proceeds as follows.

(P4 with $\nu = 1$, $[c] = 1$, and $V.a = "x"$)

(P5 with $\nu = 2$, $[c] = 2$, and $C.a = "2"$)

(P7 with $\nu = 3$, $\mu_1 = 1$, $\mu_2 = 2$, $[c] = 3$,
 $\mathbf{v}_{\mu_1}.a = "\dot{v}_1 = \dot{x}; v_1 = x;"$,
 $\mathbf{v}_{\mu_2}.a = "\dot{v}_2 = 0; v_2 = 2;"$,
 $[\mathbf{v}_{\mu_1}.j] = 1$, $O.a = " * "$, and $[\mathbf{v}_{\mu_2}.j] = 2$)

(P6 with $\nu = 4$, $[c] = 4$,
 $\mathbf{v}_{\nu-1}.a = "\dot{v}_1 = \dot{x}; v_1 = x;"$
 $\dot{v}_2 = 0; v_2 = 2;$
 $\dot{v}_3 = \dot{v}_1 * v_2 + v_1 * \dot{v}_2; v_3 = v_1 * v_2;"$,
 $F.a = " \sin "$, and $[\mathbf{v}_{\nu-1}.j] = 3$)

(P3 with $\nu = 5$,
 $\mathbf{v}_{\nu-1}.a = "\dot{v}_1 = \dot{x}; v_1 = x;"$
 $\dot{v}_2 = 0; v_2 = 2;$
 $\dot{v}_3 = \dot{v}_1 * v_2 + v_1 * \dot{v}_2; v_3 = v_1 * v_2;$
 $\dot{v}_4 = \cos(v_3) * \dot{v}_3; v_4 = \sin(v_3);"$,
 $V.a = "y"$, and $[\mathbf{v}_{\nu-1}.j] = 4$)

(P1 with $\nu = 6$,
 $\mathbf{v}_{\nu-1}.a = "\dot{v}_1 = \dot{x}; v_1 = x;"$
 $\dot{v}_2 = 0; v_2 = 2;$

$$\begin{aligned} \dot{v}_3 &= \dot{v}_1 * v_2 + v_1 * \dot{v}_2; \quad v_3 = v_1 * v_2; \\ \dot{v}_4 &= \cos(v_3) * \dot{v}_3; \quad v_4 = \sin(v_3); \\ \dot{y} &= \dot{v}_4; \quad y = v_4; \end{aligned}$$

Again, the synthesized attribute `v6.a` contains the tangent-linear code after the last reduction performed in Table 1.

3.4 Intraprocedural Flow of Control

The flow of control of the tangent-linear program is the same as for the original program. Hence, any control flow statements such as loops and branches can be treated in a straight-forward fashion by simply unparsing them. In Section A we present a proof-of-concept implementation of a syntax-directed tangent-linear code generator for single subroutines using the GNU tools `flex` and `bison`. The functionality of the software is documented in Section 4. For brevity we refrain from the presentation of a corresponding formalism that does not add anything conceptually new. Obviously, the syntactic richness of the language accepted by both the scanner and the parser can be extended easily, for example, by other control-flow structures and conditional expressions.

The presence of control flow statements has a more significant impact on the syntax-directed compilation of adjoint codes which will be discussed in the second part of this series of publications.

3.5 Interprocedural Flow of Control

The reversal of interprocedural flow of control in the context of adjoint codes generated by syntax-directed translation represents a separate topic that will be discussed in the third part of this series of papers. For tangent-linear codes the presence of subroutine calls requires their replacement with calls of the corresponding tangent-linear subroutine. For example, if `foo(x, y)` implements F from Equation (1), then its call is replaced with `foo(x, \dot{x} , y, \dot{y})`. No conceptual difficulties arise in the context of syntax-directed translation.

3.6 Vector Mode, etc.

The extension to vector mode that computes

$$\dot{\mathbf{y}} = F'(\mathbf{x}) \cdot \dot{\mathbf{x}}$$

for $\dot{\mathbf{x}} \in \mathbb{R}^{n \times l}$ and, hence, $\dot{\mathbf{y}} \in \mathbb{R}^{m \times l}$ is trivial. Any tangent-linear assignment

$$\dot{v}^j = \sum_{i \prec j} c_{j,i} \dot{v}^i$$

generated so far is simply replaced by the corresponding loop over the l components of the vectors \dot{v}^j and \dot{v}^i as follows

$$\dot{v}_k^j = \sum_{i \prec j} c_{j,i} \dot{v}_k^i \quad k = 1, \dots, l \quad .$$

Obviously, this simple modification can be done in the context of syntax-directed translation. The same statement applies to the generation of tangent-linear code for the propagation of sparse gradients in sparse forward mode AD (see ADIFOR’s SparsLinC library [3]) and to codes for computing higher derivatives by propagation of truncated Taylor series [10]. In general, any transformation that simply augments the code list with additional statements whose syntax depends only on the code parsed so far fits into the current framework. However, we do not want to imply that the practical realization of these concepts needs to be straight-forward. Often enough the technical details require sophisticated algorithmic solutions and a high level of proficiency in computer programming.

4 Implementation

The source of our simple proof-of-concept implementation (called `sdtlc` for syntax-directed tangent-linear code compiler) that uses the compiler tools `flex`⁶ and `bison`⁷ is shown in Section A. It is meant to serve as a starting point for further development of a syntax-directed tangent-linear code compiler that covers larger fractions of C and possibly C++. Moreover, given an LALR(1) grammar of some imperative programming language the generation of tangent-linear code becomes conceptually easy. We provide the source code on the project’s website to support potential other development projects in this direction.

In the following we present a small case study that is supposed to illustrate the current functionality of `sdtlc`.

Listing 1.1 shows a small input file that needs to be transformed into tangent-linear code.

Listing 1.1. `test.in`

```

1 t=0;
2 while (x<t) {
3     if (x<y) {
4         x=y+1;
5     }
6     x=sin(x*y);
7 }
```

We call `sdtlc test.in > test.out` to obtain the output in Listing 1.2.

Listing 1.2. `test.out`

```

1 double v1, v1_;
2 double v2, v2_;
3 double v3, v3_;
4 double v4, v4_;
5 v1_=0; v1=0;
6 t_=v1_; t=v1;
7 while (x<t) {
8     if (x<y) {
9         v1_=y_; v1=y;
10        v2_=0; v2=1;
11        v3_=v1_+v2_; v3=v1+v2;
12        x_=v3_; x=v3;
13    }
```

⁶ <http://www.gnu.org/software/flex/>

⁷ <http://www.gnu.org/software/bison/>

```

14 v1_=x_; v1=x;
15 v2_=y_; v2=y;
16 v3_=v1_*v2+v1*v2_; v3=v1*v2;
17 v4_=cos(v3)*v3_; v4=sin(v3);
18 x_=v4_; x=v4;
19 }

```

To verify the correctness of the transformation we provide a driver that compares the values of the two gradient entries as computed by the tangent-linear code with an approximation obtained by applying forward finite differences. The driver contains wrappers for the original code and the tangent-linear code in the form of the subroutines `test` and `test_`.

Listing 1.3. test.cpp

```

1 #include <cmath>
2 #include <iostream>
3
4 using namespace std;
5
6 void test ( double &x, double y) {
7     double t;
8     #include "test.in"
9 }
10
11 void test_ ( double &x, double& x_, double y, double y_) {
12     double t, t_;
13     #include "test.out"
14 }
15
16 int main() {
17
18     cout << "finite differences:" << endl;
19     double h=1e-6, x=-.5, y=-5., x_=x+h, y_=y;
20     test(x,y);
21     test(x_,y_);
22     cout << "dx/dx=" << (x_-x)/h << endl;
23
24     x=-.5, x_=x, y_=y+h;
25     test(x,y);
26     test(x_,y_);
27     cout << "dx/dy=" << (x_-x)/h << endl;
28
29     cout << "tangent-linear code:" << endl;
30     x=-.5, x_=1., y_=0.;
31     test_(x,x_,y,y_);
32     cout << "dx/dx=" << x_ << endl;
33
34     x=-.5, x_=0., y_=1.;
35     test_(x,x_,y,y_);
36     cout << "dx/dy=" << x_ << endl;
37
38     return 0;
39 }

```

The result of running the corresponding executable is shown below.

```

finite differences:
dx/dx=4.00571
dx/dy=0.400572

```



```
tangent-linear code:  
dx/dx=4.00572  
dx/dy=0.400572
```

Additional test cases can be found on the project's website.

5 Conclusion and Outlook

This paper discussed the automatic generation of tangent-linear code by single-pass source transformation AD without building an internal representation of the program. For the presentation of the formalism we have focused on assignment statements as the relevant syntactical units for semantic transformation. Control-flow statements are simply unparsed. The proposed approach is relatively simple to implement and generalize for full programming languages.

A substantial draw-back of this method is the missing static program analysis. An internal representation in form of a control flow graph on top of an implementation of the AST is required. The source transformation problem becomes much more complicated as it involves the development of a complete compiler front-end in addition to domain-specific data flow analyses [11]. However, it appears to be useful to apply the syntax-directed approach as much as possible during the first pass of a source transformation AD tool. The internal representation that becomes the subject of program analysis could already be that of a tangent-linear code. Thus, the optimization of this code amounts to the application of state-of-the-art compiler optimizations driven by domain-specific information, such as vanishing total derivatives of passive variables [11]. Preaccumulation of partial derivatives at the statement or basic block levels can be achieved by extending the syntax-directed approach by assembly of statically available parts of the code list (see [3], [15], and [18]). Pushing the limits of this method is the subject of ongoing research.

In part II of this series of papers we consider the syntax-directed generation of adjoint codes. A reversal of the data flow and hence also of the control flow is required. Both can be achieved during a single-pass compilation, leading to codes that enable us to compute derivatives independent of the dimension of the input space. Established applications for adjoint numerical codes are large-scale nonlinear optimization and numerical inverse methods in general. See [5] for a collection of recent activities in these areas.

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A A Proof-of-Concept Implementation

A.1 ast.h

The parser generator `bison` is told to use AST vertices of type `astNodeType` to enable the propagation of the synthesized attribute `a` based on code list indexes `j`.

Listing 1.4. `ast.h`

```

1 typedef struct {
2     char* a;
3     int j;
4 } astNodeType;
5
6 #define YYSTYPE astNodeType

```

A.2 scanner.l

Listing 1.5. `scanner.l`

```

1 %{
2 #include "ast.h"
3 #include "parser.tab.h"
4 %}
5
6 whitespace      [ \t\n]+
7 symbol          [a-z]
8 const           [0-9]
9
10 %%
11
12 {whitespace} { }
13 "if" { return IF; }
14 "while" { return WHILE; }
15 "sin" { return SIN; }
16 {symbol} {
17     yylval.a = (char*)malloc(2*sizeof(char));
18     strcpy(yylval.a,yytext);
19     return SYMBOL;
20 }
21 {const} {
22     yylval.a = (char*)malloc((strlen(yytext)+1)*sizeof(char));
23     strcpy(yylval.a,yytext);
24     return CONSTANT;
25 }
26
27 . { return yytext[0]; }
28
29 %%

```

```

30
31 void lexinit(FILE *source)
32 {
33     yyin=source;
34 }

```

A.3 parser.y

Listing 1.6. parser.y

```

1  %{
2
3  #include <stdlib.h>
4  #include <stdio.h>
5  #include <string.h>
6  #include <math.h>
7  #include "ast.h"
8
9  extern int yylex();
10 extern void lexinit(FILE*);
11
12 static int c, cmax=1;
13
14  %}
15
16 %token SYMBOL CONSTANT SIN IF WHILE
17
18 %left '+'
19 %left '*'
20
21 %%
22
23 code : sequence_of_statements
24     {
25         // print declarations of auxillary variables
26         for (c=1;c<cmax;c++) printf("double v%d, v%d_;\n",c,c);
27         // print tangent-linear code
28         printf("%s", $1.a);
29         free($1.a);
30     }
31 ;
32 sequence_of_statements : statement
33     {
34         $$=$1;
35     }
36 | statement sequence_of_statements
37     {
38         $$ .a=(char*) malloc (( strlen($1.a)+strlen($2.a)+1)*sizeof(char));
39         sprintf($$.a,"%s%s", $1.a,$2.a);
40         free($2.a); free($1.a);
41     }
42 ;
43 statement : assignment { $$=$1; }
44 | if_statement { $$=$1; }
45 | while_statement { $$=$1; }
46 ;
47 if_statement : IF '(' condition ')' '{' sequence_of_statements '}'
48     {
49         $$ .a=(char*) malloc (( strlen($3.a)+strlen($6.a)+11)*sizeof(char));
50         sprintf($$.a," if (%s) {\n%s}\n", $3.a, $6.a);

```

```

51     free($3.a); free($6.a);
52 }
53 ;
54 while_statement : WHILE '(' condition ')' '{ sequence_of_statements
                    '}'
55 {
56     $$ .a=(char*) malloc (( strlen($3.a)+strlen($6.a)+14)*sizeof(char));
57     sprintf($$.a," while (%s) {\n%s}\n", $3.a, $6.a);
58     free($3.a); free($6.a);
59 }
60 ;
61 condition : SYMBOL '<' SYMBOL
62 {
63     $$ .a=(char*) malloc (( strlen($1.a)+strlen($3.a)+2)*sizeof(char));
64     sprintf($$.a,"%s<%s", $1.a, $3.a);
65     free($1.a); free($3.a);
66 }
67 ;
68 assignment : SYMBOL '=' { c=1; } expression ';'
69 {
70     $$ .a=(char*) malloc (
71         (strlen($4.a)+2*strlen($1.a)+2*$4.j%10+13)*sizeof(char));
72     sprintf($$.a,"%s%s_=%v%d; %s=v%d;\n", $4.a, $1.a, $4.j, $1.a, $4.j);
73     free($1.a); free($4.a);
74 }
75 ;
76 expression : expression '*' expression
77 {
78     $$ .a=(char*) malloc (
79         (strlen($1.a)+strlen($3.a)+2*c%10+3*$1.j%10+3*$3.j%10+30)*
            sizeof(char));
80     $$ .j=c++; if (c>cmax) cmax=c;
81     sprintf($$.a,"%s%sv%d_=%v%d_*v%d+v%d*v%d; v%d=v%d*v%d;\n",
82         $1.a, $3.a, $$ .j, $1.j, $3.j, $1.j, $3.j, $$ .j, $1.j, $3.j);
83     free($1.a); free($3.a);
84 }
85 | expression '+' expression
86 {
87     $$ .a=(char*) malloc (
88         (strlen($1.a)+strlen($3.a)+2*c%10+2*$1.j%10+2*$3.j%10+24)*
            sizeof(char));
89     $$ .j=c++; if (c>cmax) cmax=c;
90     sprintf($$.a,"%s%sv%d_=%v%d_+v%d; v%d=v%d+v%d;\n",
91         $1.a, $3.a, $$ .j, $1.j, $3.j, $$ .j, $1.j, $3.j);
92     free($1.a); free($3.a);
93 }
94 | SIN '(' expression ')'
95 {
96     $$ .a=(char*) malloc (( strlen($3.a)+2*c%10+3*$3.j%10+30)*sizeof(
97         char));
98     $$ .j=c++; if (c>cmax) cmax=c;
99     sprintf($$.a,"%sv%d_=%cos(v%d)*v%d; v%d=sin(v%d);\n",
100         $3.a, $$ .j, $3.j, $3.j, $$ .j, $3.j);
101     free($3.a);
102 }
103 | SYMBOL
104 {
105     $$ .a=(char*) malloc ((2*c%10+2*strlen($1.a)+13)*sizeof(char));
106     $$ .j=c++; if (c>cmax) cmax=c;

```

```

106     sprintf($$.a,"v%d_=%s_ ; v%d=%s;\n",$$.j,$1.a,$$.j,$1.a);
107     free($1.a);
108 }
109 | CONSTANT
110 {
111     $$ .a=(char*) malloc ((2*c%10+strlen($1.a)+13)*sizeof(char));
112     $$ .j=c++; if (c>cmax) cmax=c;
113     sprintf($$.a,"v%d_=0; v%d=%s;\n",$$.j,$$.j,$1.a);
114     free($1.a);
115 }
116 ;
117
118 %%
119
120 int yyerror(char *msg) { printf("ERROR: %s \n",msg); return -1; }
121
122 int main(int argc , char* argv [])
123 {
124     FILE *source_file = fopen(argv[1] , "r");
125     lexinit(source_file);
126     yyparse();
127     fclose(source_file);
128     return 0;
129 }

```

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